

Primal problem

$$\begin{aligned}
 [\min]_z &= 3x_1 + 5x_2 - 2x_3 - x_4 + 0x_5 + 0x_6 \\
 \text{s. to} \quad &x_1 + 2x_2 + 2x_3 + x_5 = 10 \\
 &2x_1 - x_2 + 3x_4 + x_6 = 5 \\
 &\text{with } \mathbf{x} \geq 0
 \end{aligned}$$

	Decision Variable	Solution Value	Unit Cost or Profit c(j)	Total Contribution	Reduced Cost	Basis Status	Allowable Min. c(j)	Allowable Max. c(j)
1	X1	0	3,0000	0	4,6667	at bound	-1,6667	M
2	X2	0	5,0000	0	6,6667	at bound	-1,6667	M
3	X3	5,0000	-2,0000	-10,0000	0	basic	-M	0
4	X4	1,6667	-1,0000	-1,6667	0	basic	-21,0000	0
5	X5	0	0	0	1,0000	at bound	-1,0000	M
6	X6	0	0	0	0,3333	at bound	-0,3333	M
	Objective	Function	(Min.) =	-11,6667				
	Constraint	Left Hand Side	Direction	Right Hand Side	Slack or Surplus	Shadow Price	Allowable Min. RHS	Allowable Max. RHS
1	C1	10,0000	=	10,0000	0	-1,0000	0	M
2	C2	5,0000	=	5,0000	0	-0,3333	0	M

Dual problem (“asymmetric” dual)

$$\begin{aligned}
 [\max]_w &= 10y_1 + 5y_2 \\
 \text{s. to} \quad &y_1 + 2y_2 \leq 3 \\
 &2y_1 - y_2 \leq 5 \\
 &2y_1 \leq -2 \\
 &3y_2 \leq -1 \\
 &y_1 \leq 0 \\
 &y_2 \leq 0 \\
 &\text{with } \mathbf{y} \text{ free}
 \end{aligned}$$

	Decision Variable	Solution Value	Unit Cost or Profit c(j)	Total Contribution	Reduced Cost	Basis Status	Allowable Min. c(j)	Allowable Max. c(j)
1	C1	-1,0000	10,0000	-10,0000	0	at bound	-M	10,0000
2	C2	-0,3333	5,0000	-1,6667	0	at bound	-M	5,0000
	Objective	Function	(Max.) =	-11,6667	(Note:	Alternate	Solution	Exists!!)
	Constraint	Left Hand Side	Direction	Right Hand Side	Slack or Surplus	Shadow Price	Allowable Min. RHS	Allowable Max. RHS
1	X1	-1,6667	<=	3,0000	4,6667	0	-1,6667	M
2	X2	-1,6667	<=	5,0000	6,6667	0	-1,6667	M
3	X3	2,0000	>=	2,0000	0	-5,0000	0	M
4	X4	1,0000	>=	1,0000	0	-1,6667	0	21,0000
5	X5	-1,0000	<=	0	1,0000	0	-1,0000	M
6	X6	-0,3333	<=	0	0,3333	0	-0,3333	M

To a **positive shadow price** corresponds an **active constraint**, and to a **non-active constraint** corresponds a **null shadow price**.

