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Previous chapter discussed memory. This chapter presents:

- semiconductor main memory subsystems.
  - ROM;
  - DRAM;
  - SRAM memories
- error control techniques used to enhance memory reliability
- more advanced DRAM architectures;
But why do we need these types of memories? Any ideas?
But why do we need these types of memories? Any ideas?

- Remember these guys?
But why do we need these types of memories? Any ideas?

- Remember these guys?

- Serial memory takes different lengths of time to access information:
  - depends on where the desired location is relative to the current position;
Memory is a collection of **cells** with the following properties:

- They exhibit two stable states, used to represent binary 1 and 0;
- They are capable of being written into (at least once), to set the state;
- They are capable of being read to sense the state;
- Access time is the same regardless of the location;
Cell has three terminals capable of carrying an electrical signal:

- **select**: selects a memory cell for a read / write operation;
- **control**: indicates whether a read / write operation is being performed;
- **read/write**:
  - For writing, terminal sets the state of the cell to 1 or 0.
  - For reading, terminal is used for output of the cell’s state.

---

**Figure: Memory cell write operation (Source: (Stallings, 2015))**

**Figure: Memory cell read operation (Source: (Stallings, 2015))**
Example

Consider, a memory with a capacity of 1K words of 16 bits each:

- **Capacity:**
  - \(1K \times 16 = 16Kbits = 2Kbytes\);

- **Each word has an address:**
  - 0 to 1023

- **When a word is read or written:**
  - memory acts on all 16 bits;

\[
\begin{array}{c|c|c}
\text{Memory Address} & \text{Binary} & \text{Decimal} \\
\hline
0000000000 & 0 & 10110101 01011100 \\
0000000001 & 1 & 10101011 10001001 \\
0000000010 & 2 & 00011010 01001110 \\
& \cdots & \cdots \\
1111111101 & 1021 & 10011101 00010101 \\
1111111110 & 1022 & 00011010 00111110 \\
1111111111 & 1023 & 11011110 00100100 \\
\end{array}
\]

Figure: Contents of a 1024 x 16 memory (Source: (Mano and Kime, 2007))
Based on these concepts how do you think a write operation works? Any ideas?
Write operation steps:

1. Apply the binary address of the desired word to the address lines.

2. Apply the data bits that must be stored in memory to the data input lines.

3. Activate the Write control line.

Memory unit will then transfer the bits to that address.
Based on these concepts how do you think a read operation works? Any ideas?
Read operation steps:

1. Apply the binary address of the desired word to the address lines.
2. Activate the Read control line.
3. Memory unit will then transfer the bits to the data output lines.
Memory unit operation is controlled by an external device (1/2):

- CPU is synchronized by its own clock pulses;
- Control signals are employed for memory read / write.
  - **Access time** - time required for specifying an address and obtaining the word;
  - **Write time** - time required for specifying an address and storing the word;
- CPU must provide the control signals
Memory unit operation is controlled by an external device (2/2):

- CPU provides the control signals synchronized with its clock:
- This implies that:
  - read / write operations will take a certain number of clock periods;
- What does this mean? Let's see with an example =)
Assume:

- CPU with a clock frequency of 50 Mhz;
- Memory access time: 65 ns;
- Memory write time: 75 ns

How many clock pulses do we need for read / write operations?
CPU with a clock frequency of 50 Mhz:

- How long does one clock pulse take? Any Ideas?

\[
\begin{align*}
\text{CPU with a clock frequency of 50 Mhz:} \\
\text{• How long does one clock pulse take? Any Ideas?} \\

f &= \frac{1}{p} \Leftrightarrow \\
p &= \frac{1}{f} \Leftrightarrow \\
p &= \frac{1}{50\text{ Mhz}} \Leftrightarrow \\
p &= \frac{1}{50 \times 10^6\text{ hz}} \Leftrightarrow \\
p &= 2 \times 10^{-8}\text{ s} \Leftrightarrow 20\text{ ns}
\end{align*}
\]
Example (3/7)

- CPU clock pulse: 20ns;
- Assume:
  - Memory access time: 65ns;
  - Memory write time: 75ns

How many clock pulses do we need for read / write operations?

- 4 clock pulses for read / write operations;
Example (4/7)

For the **write operation**:

![Write cycle diagram](image)

Figure: Write cycle (Source: (Mano and Kime, 2007))
Example (5/7)

For the **write operation**:

1. CPU must provide the address (T1 pulse);
2. Memory enable is set (T1 pulse);
3. Data is supplied (T2 pulse);
4. *Read/Write* signal set to 0 for write operation (T2 pulse):
   - CPU waits for T2 to let the address signals stabilize:
     - Otherwise: wrong address may be used!
   - Signal must stay activated long enough for the operation to finish;
5. When T4 completes, write operation has ended with 5ns to spare
Example (6/7)

For the **read operation**:

![Timing Waveforms]

Figure: Read cycle (Source: Mano and Kime, 2007)
For the **read operation**:

1. CPU must provide the address (T1 pulse);

2. Memory enable is set (T1 pulse);

3. **Read/Write** signal set to 1 for read operation (T2 pulse):
   - Signal must stay activated long enough for the operation to finish;
   - Selected word is placed onto the data output lines;

4. When T4 completes, write operation has ended with 15ns to spare
Major types of semiconductor memory

Let's have a look at the different types of memory technologies:

<table>
<thead>
<tr>
<th>Memory Type</th>
<th>Category</th>
<th>Erasure</th>
<th>Write Mechanism</th>
<th>Volatility</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random-access memory (RAM)</td>
<td>Read-write memory</td>
<td>Electrically, byte-level</td>
<td>Electrically</td>
<td>Volatile</td>
</tr>
<tr>
<td>Read-only memory (ROM)</td>
<td>Read-only memory</td>
<td>Not possible</td>
<td>Masks</td>
<td></td>
</tr>
<tr>
<td>Programmable ROM (PROM)</td>
<td>Read-only memory</td>
<td>Not possible</td>
<td>Masks</td>
<td></td>
</tr>
<tr>
<td>Erasable PROM (EPROM)</td>
<td>Read-mostly memory</td>
<td>UV light, chip-level</td>
<td>Electrically</td>
<td></td>
</tr>
<tr>
<td>Electrically Erasable PROM (EEPROM)</td>
<td>Read-mostly memory</td>
<td>Electrically, byte-level</td>
<td>Electrically</td>
<td>Nonvolatile</td>
</tr>
<tr>
<td>Flash memory</td>
<td></td>
<td>Electrically, block-level</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure: Semiconductor memory types (Source: (Stallings, 2015))
Random-access memory

- Randomly access any possible address;
- Possible both to read and write data;
- Volatile: requires a power supply;
- For a chip with $m$ words with $n$ bits per word:
  - Consists of an array with $m \times n$ binary storage cells
- *E.g.*: DRAM and SRAM.
  - Lets have a look at these =)
Dynamic RAM (DRAM)

Made with **cells** that store data as charge on capacitors:

- Capacitor charge presence or absence is interpreted as a binary 1 or 0;
- Capacitors have a natural tendency to discharge;
- Requires periodic charge refreshing to maintain data storage
DRAM Cell components:

If voltage goes to the address line:

- **Transistor closes:**
  - Current flows to capacitor;

If no voltage goes to the address line:

- **Transistor opens:**
  - No current flows to capacitor;

Figure: DRAM Cell (Source: [Stallings, 2015])
Based on the DRAM cell components:

How do you think a write operation works? Any ideas?

Figure: DRAM Cell (Source: (Stallings, 2015))
Write operation:

1. Voltage signal is applied to the bit line
   - Low voltage = 0;
   - High voltage = 1;

2. A signal is then applied to the address line:
   - transistor closes...
   - ...charge goes to the capacitor.

Figure: DRAM Cell (Source: [Stallings, 2015])
Based on the DRAM cell components:

How do you think a read operation works? Any ideas?

Figure: DRAM Cell (Source: Stallings, 2015)
**Read operation:**

1. Address line is activated
2. Transistor turns on
3. Capacitor charge goes to bit line...;
   - ...Low voltage = 0
   - ...High voltage = 1
4. Cell readout discharges the capacitor:
   - state must be restored;

![Dynamic RAM Cell](image)

**Figure:** Dynamic RAM Cell (Source: (Stallings, 2015))
Besides DRAM...

Do you have any idea of other type of technology that can be employed? Any ideas?

- Maybe based on something that we saw earlier in the semester...
Static RAM (SRAM)

Binary values are stored using **SR flip-flop** configurations:

- Remember flip-flops? We saw them at the beginning of the semester...
- Same logic elements used in the processor registers;
- will hold its data as long as power is supplied to it.
Cell storage is modelled by an SR flip-flop:

![SR Flip-flop Diagram](image)

**Figure: SRAM Cell (Source: (Mano and Kime, 2007))**

<table>
<thead>
<tr>
<th>S</th>
<th>R</th>
<th>Q_{n+1}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>Q_n</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>—</td>
</tr>
</tbody>
</table>

**Figure: SR Flip flop table (Source: (Stallings, 2015))**

- **Flip-flop inputs** are enabled by a **select** (S) signal:
  - $S = 0$, stored content is held;
  - $S = 1$, stored content is determined by $B$ and $\overline{B}$

- **Flip-flop outputs** are enabled by a **select** (S) signal:
  - $S = 0$, both $C$ and $\overline{C}$ are 0;
  - $S = 1$, $C$ is the stored value and $\overline{C}$ is its complement.
How to choose between DRAM and SRAM? Any ideas?

- What are the pros / cons of DRAM?
- What are the pros / cons of SRAM?
DRAM vs SRAM (1/5)

- Both are volatile:
  - power must be continuously supplied to preserve the bit values;

- DRAMs:
  - Periodically refresh capacitor’s charge;

- SRAM:
  - No need to periodically refresh;
DRAM vs SRAM (2/5)

- DRAM cell is simpler and smaller than a SRAM cell:
  - (1 transistor, 1 capacitor) vs. SR flip-flop
  - DRAM is denser (smaller cells = more cells per unit area)
  - Due to its simplicity:
    - DRAM is cheaper than corresponding SRAM;
DRAM vs SRAM (3/5)

- DRAM requires the supporting refresh circuitry (readout):
  - This is a fixed cost, does not increase with size =)
  - This cost is more than compensated by the smaller cost of DRAM cells;
  - Thus, DRAMs tend to be favoured for large memory requirements;
SRAMs are faster and more expensive than DRAMs

- No need to refresh the circuitry after a readout;

Because of these characteristics:

- **DRAM**: used in main memory;
- **SRAM**: used in cache;
### DRAM vs SRAM (5/5)

<table>
<thead>
<tr>
<th>Memory technology</th>
<th>Typical access time</th>
<th>$ per GiB in 2012</th>
</tr>
</thead>
<tbody>
<tr>
<td>SRAM semiconductor memory</td>
<td>0.5–2.5 ns</td>
<td>$500–$1000</td>
</tr>
<tr>
<td>DRAM semiconductor memory</td>
<td>50–70 ns</td>
<td>$10–$20</td>
</tr>
<tr>
<td>Flash semiconductor memory</td>
<td>5,000–50,000 ns</td>
<td>$0.75–$1.00</td>
</tr>
<tr>
<td>Magnetic disk</td>
<td>5,000,000–20,000,000 ns</td>
<td>$0.05–$0.10</td>
</tr>
</tbody>
</table>

Figure: Access time and price per bit (Source: (Patterson and Hennessy, 2013))
Read-only memory (ROM)

- Contains a permanent pattern of data that cannot be changed;
  - Therefore:
    - Possible to read a ROM;
    - **Not possible to write data more than once**;

- Advantage:
  - Data / Program is permanently in main memory;
  - No need to load from a secondary storage device;
  - Original BIOS were stored in ROM chips.

- Nonvolatile: no power source is required;
Not possible to write data more than once:

- Data is wired into the chip as part of the fabrication process
- Data insertion is expensive;
- No room for error:
  - If one bit is wrong, the whole batch of ROMs must be thrown out.
  - =’( 
Different types of ROM (1/4):

- **Programmable ROM (PROM):**
  - nonvolatile and may be written into only once;
  - Writing may be performed at a later time than the original chip fabrication.
  - Special equipment is required for the writing process;
  - More expensive than ROM;
Different types of ROM (2/4):

- **Erasable programmable read-only memory (EPROM):**
  - Can be altered multiple times;
  - **Entire memory contents need to be erased**;
  - Special equipment is required for the erasure process:
    - Ultra-violet radiation;
  - Slow erasure procedure (>20 minutes);
  - More expensive than PROM;
Different types of ROM (3/4):

- **Electrically erasable programmable read-only memory (EEPROM):**
  - Can be altered multiple times;
  - Special equipment is required for the erasure process:
    - No need to erase prior contents...
    - ...only the byte or bytes addressed are updated.
    - Ultra-violet radiation;
  - Faster erasure procedure than EPROM;
  - More expensive than EPROM;
Different types of ROM (4/4):

- **Flash memory:**
  - named because of the speed with which it can be reprogrammed;
  - between EPROM and EEPROM in both cost and functionality:
    - Uses an electrical erasing technology;
    - Possible to erase blocks of memory;
    - Does not provide byte-level erasure;
  - Technology used in pendrives;
Now that we have seen the core memory concepts:

How can we organize these concepts into a functional memory unit? Any ideas?
Typical organization of a 16-Mbit DRAM:

Figure: Typical 16 Megabit DRAM (4M × 4) (Source: Stallings, 2015)
In the case of the previous picture (1/4):

- 4 bits are read or written at a time
- Memory array is organized as four arrays of 2048 by 2048 elements;
- Address lines supply the address of the word to be selected;
  - $\log_2 W$ lines are needed;
  - *E.g.*, 11 address lines are needed to select one of 2048 rows;
- These lines are fed into a row decoder;
- Decoder activates a single line of memory;
In the case of the previous picture (2/4):

- The same procedure is applied to select columns;
- Note that there are only 11 address lines ($A_0 - A_{10}$):
  - Half the number you would expect for a $2048 \times 2048$ array.
- First, a row address select ($RAS$) signal is emitted:
  - to define the row address of the array
- Second, a column address select ($CAS$) signal is emitted:
  - to define the column address of the array
In the case of the previous picture (3/4):

- **Write enable** \((\overline{WE})\) signal
  - specifies that a **write** operation is to be performed;

- **Output enable** \((\overline{OE})\)
  - signal specifies that a **read** operation is to be performed;
In the case of the previous picture (4/4):

- Refreshing technique:
  - Refresh counter: step through all of the row values;
  - For each line:
    - Memory row is chosen;
    - RAS line is activated;
    - Data are read out and written back into the same location
Let's look at a simplified example:

Figure: 256KByte memory organization (Source: [Stallings, 2015])
In the case of the previous picture:

- Shows a memory module consisting of 256K 8-bit words;

- For 256K words, an 18-bit address is needed
  - Memory Address Register containing:
    - 9 bits for line selection;
    - 9 bits for column selection;

- Address is presented to 8 256K 1-bit chips:
  - each of which provides the input/ output of 1 bit.

- Memory Buffer Register of 8-bits:
  - Where data is read from;
  - Where data is written to;
And that concludes the semiconductor memory section... Yay!!!

- Next topic please =)
Semiconductor memory systems are subject to errors (1/2):

**Hard Failures:**

- **Permanent physical defect;**

- Damaged memory cell(s) cannot reliably store data:
  - become stuck at 0 or 1 or...
  - ...switch erratically between 0 and 1

- Caused by:
  - Harsh environmental abuse;
  - Manufacturing defects;
  - Wear and tear;
Semiconductor memory systems are subject to errors (2/2):

**Soft Failures:**

- **Random, nondestructive event**
  - Alters the contents of one or more memory cells
    - Without damaging the memory.
  - Caused by:
    - Power supply problems;
    - Alpha particles (radioactive decay).
Hard and soft errors are clearly undesirable...

So what can we do to address them? Any ideas?
Hard and soft errors are clearly undesirable...

So what can we do to address them? Any ideas?

- Idea: algorithms for both detecting and correcting errors ;)

Luis Tarrataca

Chapter 5 - Internal Memory
General method

Figure: Error correcting code function (Source: (Stallings, 2015))
From the previous picture (1/3):

1. $M$-bit data is to be written into memory;
2. Computation $f(M)$ is performed on the data ($K$ check bits);
3. Both the data and the code ($M + K$ bits) are stored in memory;
From the previous picture (2/3):

4. Eventually, the stored word will be read out;

5. Computation $f(M)$ is again performed on the data ($K$ check bits);

6. A comparison is made between both check bits;
From the previous picture (3/3):

The comparison yields one of three results:

1. No errors are detected:
   - Fetched data bits are sent out;

2. An error is detected, and it is possible to correct the error:
   - Data bits plus error correction bits are fed into a corrector
   - Producing a corrected set of $M$ bits to be sent out.

3. An error is detected, but it is not possible to correct it:
   - =’( This condition is reported.
Guess what we will be seeing next?
Guess what we will be seeing next?

- Error-correcting codes =)
- High-probability of appearing in the next exam... ;)
- Lets start with a basic example...
Hamming code

Simplest of the error-correcting codes:

Let's see an example on 4-bits:

1. Data = \{1, 1, 1, 0\}

2. Uses Venn diagrams;

3. Three intersecting circles → seven compartments;

4. We assign the 4 data bits to the inner compartments

Figure: Hamming error correcting code (Source: (Stallings, 2015))
Hamming code

Simplest of the error-correcting codes:

5. Other compartments filled with parity bits;

6. What is a parity bit?
   - Total number of 1s in circle must be even;

7. Parity values:
   - Circle A = three data 1s, parity bit is 1;
   - Circle B = two data 1s, parity bit is 0;
   - Circle C = two data 1s, parity bit is 0;

Figure: Hamming error correcting code (Source: Stallings, 2015)
Hamming code

Simplest of the error-correcting codes:

8. Imagine an error changes one of the data bits
   - See new figure

9. Check parity bits:
   - \( C_A = \) two data 1s, parity bit is 1 should be 0;
   - \( C_B = \) two data 1s, parity bit is 0 should be 0;
   - \( C_C = \) one data 1s, parity bit is 0 should be 1;

10. Therefore:
   - error: intersection of A with C, excluding B

Figure: Hamming error correcting code (Source: [Stallings, 2015])
Hamming code

Simplest of the error-correcting codes:

11 Error can be corrected by changing that bit.

Figure: Hamming error correcting code (Source: [Stallings, 2015])
Ok, we saw an example for 4 bits...

How can we extend this to any number of bits?
Example code to detect and correct single-bit errors in 8-bit words:

- Error code is calculated twice (check\textsubscript{1} and check\textsubscript{2}) (Slide 60)

- Bit-by-bit comparison is done by performing XOR (⊕):

<table>
<thead>
<tr>
<th></th>
<th>b\textsubscript{7}</th>
<th>b\textsubscript{6}</th>
<th>b\textsubscript{5}</th>
<th>b\textsubscript{4}</th>
<th>b\textsubscript{3}</th>
<th>b\textsubscript{2}</th>
<th>b\textsubscript{1}</th>
<th>b\textsubscript{0}</th>
</tr>
</thead>
<tbody>
<tr>
<td>check\textsubscript{1}</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>check\textsubscript{2}</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>check\textsubscript{1} ⊕ check\textsubscript{2}</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
</tbody>
</table>

- Result is called the \textit{syndrome word}:
  - A zero bit means a match;
  - A one bit means a mismatch;
Syndrome word will have $K$-bits

- Syndrome has a range between 0 and $2^K - 1$;
- If syndrome has value 0, no error was detected;
- Otherwise, $2^K - 1$ values to indicate which bit was in error;
 Syndrome word will have $K$-bits

- Syndrome has a range between 0 and $2^K - 1$;
- If syndrome has value 0, no error was detected;
- Otherwise, $2^K - 1$ values to indicate which bit was in error;

But how large should $K$ be?
But how large should $K$ be?

- We know that there should exist:
  - $2^K - 1$ combinations to indicate where the error is.

- Therefore, if we have $M$-bit words:
  - $2^K - 1$ should be large enough to encode one of the $M$ available positions;
    - Error can be in position 0;
    - Error can be in position 1;
    - ...;
    - Error can be in position $M - 1$;
  - i.e.: $2^K - 1 \geq M;$
But what happens if we have an error in the $K$ check bits?

Error can be:

- As before in one of the original $M$ positions;
- But now we also need to consider $K$ positions;
- $i.e.: 2^K - 1 \geq M + K;$
For 8 data bits, 4 check bits are required, representing an increase of 50%.

- \[ K = 3 : 2^3 - 1 < 8 + 3 \]
- \[ K = 4 : 2^4 - 1 \geq 8 + 4 \]
We would like to generate a syndrome with the following characteristics:

- If the syndrome contains all 0s:
  - No error has been detected.

- If the syndrome contains one and only one bit set to 1:
  - Then an error has occurred in one of the check bits
  - No correction is needed;

- If the syndrome contains more than one bit set to 1:
  - Then the syndrome value indicates the position of the data bit in error.
  - This data bit is inverted for correction.
Data (8-bit) and syndrome (4-bit) are arranged into a 12-bit word:

<table>
<thead>
<tr>
<th>Bit position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td>D8</td>
<td>D7</td>
<td>D6</td>
<td>D5</td>
<td>D4</td>
<td>D3</td>
<td>D2</td>
<td>D1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Check bit</td>
<td>C8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>C4</td>
<td></td>
<td></td>
<td>C2</td>
<td></td>
<td></td>
<td>C1</td>
</tr>
</tbody>
</table>

Figure: Layout of data bits and check bits (Source: (Stallings, 2015))

1. Bit positions that are powers of 2 are designated as check bits;
2. Bit positions that are not power of 2 are designated as data bits;
3. Each **check bit** operates on every **data bit** whose position number:
   - contains a 1 in the same bit position as the position number of that check bit.

4. *E.g.*: Check bit 1 operates on:
   - Data bit 1 (0011), since it has a 1 in position 1;
   - Data bit 2 (0101), since it has a 1 in position 1;
   - Data bit 4 (0101), since it has a 1 in position 1;
   - Data bit 5 (1001), since it has a 1 in position 1;
   - Data bit 7 (1011), since it has a 1 in position 1;

5. *I.e.*: $C_1 = D_1 \oplus D_2 \oplus D_4 \oplus D_5 \oplus D_7$
6 E.g.: Check bit 2 operates on:

- Data bit 1 (0011), since it has a 1 in position 2;
- Data bit 3 (0110), since it has a 1 in position 2;
- Data bit 4 (0111), since it has a 1 in position 2;
- Data bit 6 (1010), since it has a 1 in position 2;
- Data bit 7 (1011), since it has a 1 in position 2;

7 I.e.: $C_2 = D_1 \oplus D_3 \oplus D_4 \oplus D_6 \oplus D_7$
8 E.g.: Check bit 4 operates on:

- Data bit 2 (0101), since it has a 1 in position 3;
- Data bit 3 (0110), since it has a 1 in position 3;
- Data bit 4 (0111), since it has a 1 in position 3;
- Data bit 8 (1100), since it has a 1 in position 3;

9 I.e.: $C_4 = D_2 \oplus D_3 \oplus D_4 \oplus D_8$
10 **E.g.:** Check bit 8 operates on:

- Data bit 5 (1001), since it has a 1 in position 4;
- Data bit 6 (1010), since it has a 1 in position 4;
- Data bit 7 (1011), since it has a 1 in position 4;
- Data bit 8 (1100), since it has a 1 in position 4;

11 **I.e.:** \( C_8 = D_5 \oplus D_6 \oplus D_7 \oplus D_8 \)
Overall conclusion:

\[
\begin{align*}
C_1 & = D_1 \oplus D_2 \oplus D_4 \oplus D_5 \oplus D_7 \\
C_2 & = D_1 \oplus D_3 \oplus D_4 \oplus D_6 \oplus D_7 \\
C_4 & = D_2 \oplus D_3 \oplus D_4 \oplus D_5 \oplus D_8 \\
C_8 & = D_5 \oplus D_6 \oplus D_7 \oplus D_8
\end{align*}
\]
Example (1/5)

Let’s say that the 8-bit input word is 00111001:

<table>
<thead>
<tr>
<th>Bit position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td>D8</td>
<td>D7</td>
<td>D6</td>
<td>D5</td>
<td>D4</td>
<td>D3</td>
<td>D2</td>
<td>D1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Check bit</td>
<td>C8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>C4</td>
<td>C2</td>
<td>C1</td>
<td></td>
</tr>
</tbody>
</table>

Figure: Check bit calculation (Source: [Stallings, 2015])

- \( C_1 = D_1 \oplus D_2 \oplus D_4 \oplus D_5 \oplus D_7 = 1 \oplus 0 \oplus 1 \oplus 1 \oplus 0 = 1 \)
- \( C_2 = D_1 \oplus D_3 \oplus D_4 \oplus D_6 \oplus D_7 = 1 \oplus 0 \oplus 1 \oplus 1 \oplus 0 = 1 \)
- \( C_4 = D_2 \oplus D_3 \oplus D_4 \oplus D_8 = 0 \oplus 0 \oplus 1 \oplus 0 = 1 \)
- \( C_8 = D_5 \oplus D_6 \oplus D_7 \oplus D_8 = 1 \oplus 1 \oplus 0 \oplus 0 = 0 \)
The combined data and check bits will be stored as:

<table>
<thead>
<tr>
<th>Bit position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td>D8</td>
<td>D7</td>
<td>D6</td>
<td>D5</td>
<td>D4</td>
<td>D3</td>
<td>D2</td>
<td>D1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Check bit</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>C8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word stored as</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure: Check bit calculation (Source: [Stallings, 2015](#))
Example (3/5)

Suppose now that data bit 3 sustains an error and is changed from 0 to 1:

<table>
<thead>
<tr>
<th>Bit position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td>D8</td>
<td>D7</td>
<td>D6</td>
<td>D5</td>
<td>D4</td>
<td>D3</td>
<td>D2</td>
<td>D1</td>
<td>D1</td>
<td>D1</td>
<td>D1</td>
<td>D1</td>
</tr>
<tr>
<td>Check bit</td>
<td>C8</td>
<td></td>
<td></td>
<td></td>
<td>C4</td>
<td></td>
<td></td>
<td>C2</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word stored as</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Word fetched as</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure: Check bit calculation (Source: (Stallings, 2015))
Example (4/5)

Check bits are recalculated:

- \( C_1 = D_1 \oplus D_2 \oplus D_4 \oplus D_5 \oplus D_7 = 1 \oplus 0 \oplus 1 \oplus 1 \oplus 0 = 1 \)
- \( C_2 = D_1 \oplus D_3 \oplus D_4 \oplus D_6 \oplus D_7 = 1 \oplus 1 \oplus 1 \oplus 1 \oplus 0 = 0 \)
- \( C_4 = D_2 \oplus D_3 \oplus D_4 \oplus D_8 = 0 \oplus 1 \oplus 1 \oplus 0 = 0 \)
- \( C_8 = D_5 \oplus D_6 \oplus D_7 \oplus D_8 = 1 \oplus 1 \oplus 0 \oplus 0 = 0 \)
Example (5/5)

Syndrome is formed by comparing new check bits against old:

\[
\begin{array}{cccc}
C_8 & C_4 & C_2 & C_1 \\
0 & 1 & 1 & 1 \\
\oplus & 0 & 0 & 0 & 1 \\
\hline
0 & 1 & 1 & 0 \\
\end{array}
\]

- The result is 0110 (bit position 6) indicates that data bit 3 is in error.

Figure: Check bit calculation (Source: (Stallings, 2015))
Example 1

Fill out the table and calculate the syndrome for:

- Data stored: 11101001
- Data fetched: 01101001

<table>
<thead>
<tr>
<th>Bit Position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position Number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Check bit</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word Stored as</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word Fetched as</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
**Example 2**

Fill out the table and calculate the syndrome for:

- **Data stored**: 10011001
- **Data fetched**: 10010001

<table>
<thead>
<tr>
<th>Bit Position</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position Number</td>
<td>1100</td>
<td>1011</td>
<td>1010</td>
<td>1001</td>
<td>1000</td>
<td>0111</td>
<td>0110</td>
<td>0101</td>
<td>0100</td>
<td>0011</td>
<td>0010</td>
<td>0001</td>
</tr>
<tr>
<td>Data bit</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Check bit</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word Stored as</td>
<td></td>
<td></td>
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<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Word Fetched as</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Basic building block of main memory remains the DRAM chip:

- No significant changes in DRAM architecture from the 1970s to the 2000’s
- Traditional DRAM chip is constrained both:
  - by its internal architecture and...
  - ...by its interface to the processor’s memory bus.

So, what can be done to improve performance?
So, what can be done to improve performance?

• One or more levels of high-speed SRAM cache;

• However:
  • SRAM is costlier than DRAM;
  • Expanding cache size beyond a certain point yields diminishing returns;

• A number of enhancements have been developed:
  • SDRAM;
  • DDR-DRAM;
  • RDRAM
A performance comparison of the different types of DRAM:

<table>
<thead>
<tr>
<th></th>
<th>Clock Frequency (MHz)</th>
<th>Transfer Rate (GB/s)</th>
<th>Access Time (ns)</th>
<th>Pin Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>SDRAM</td>
<td>166</td>
<td>1.3</td>
<td>18</td>
<td>168</td>
</tr>
<tr>
<td>DDR</td>
<td>200</td>
<td>3.2</td>
<td>12.5</td>
<td>184</td>
</tr>
<tr>
<td>RDRAM</td>
<td>600</td>
<td>4.8</td>
<td>12</td>
<td>162</td>
</tr>
</tbody>
</table>

Figure: Performance comparison of some DRAM alternatives (Source: (Stallings, 2015))
SDRAM works in a **synchronous** manner:

- Data exchanges with the processor are synchronized with system clock;

- Unlike DRAM which is **asynchronous** and imposes **wait states**;

Wait, what is a wait state?
Wait, what is a wait state?

In a typical DRAM (1/2):

1. Processor presents addresses and control signals to the memory;
2. Indicating that data at an address should be read/written from/into;
3. After a delay (access time) the DRAM either writes or reads the data:
Wait, what is a wait state?

In a typical DRAM (2/2):

4. During the access-time delay DRAM performs various tasks, e.g.:
   - Activating high capacitance of the row and column lines;
   - Sensing the data;
   - Routing data out through the output buffers

5. Processor *waits* through this delay, slowing performance.
   - Thus the name *wait states*
What do you think would be an ideal method for interacting with memory? Any ideas?
Based on the previous text...

What do you think would be an ideal method for interacting with memory? Any ideas?

• Let the processor issue read / write commands;
• Memory processes these requests;
• Meanwhile the processor is able to do something else;
SDRAM advantage 1

- Processor issues data and address information to the SDRAM;
- SDRAM responds after a set number of clock cycles;
- Meanwhile the processor can perform other tasks;

![SDRAM Read Timing Diagram]

In this example:
- Processor issues read command (READ A);
- Memory has a latency of two clock cycles and 4-bits bursts;
- Meanwhile processor executes NOP instructions;

Figure: SDRAM read timing (Source: (Stallings, 2015))
Also, DRAM has the ability to transfer bits in burst:

- Several units of data are synchronously transferred onto the bus;
- Without having to specify the address of those data units;
  - No need to refresh MAR multiple times;
  - Can be done when reading multiple sequential addresses;
  - Is performed by specifying a burst length variable;
Double Data Rate SDRAM (DDR-SDRAM)

Transfers are synchronized to the system clock:

- Same as SDRAM, however:
  - SDRAM only transfers on the rising edge of the clock;
  - DDR-SDRAM transfers on the rising and the falling edge of the clock:
    - Twice the bandwidth based on the same clock rate and data width;
Advanced DRAM organization

Double Data Rate SDRAM (DDR-SDRAM)

Figure: DDR SDRAM read timing (Source: [Stallings, 2015])

RAS = Row address select
CAS = Column address select
DQ = Data (in or out)
DQS = DQ select

Figure: DDR SDRAM read timing (Source: [Stallings, 2015])
Sames as DDR-SDRAM, however:

- Lower voltage requirements, thus lower heat dissipation;
- Higher data width bus allows for higher transfer speeds;
  - Made specifically for the texture requirements of video games;

Figure: Geforce GTX 1080

Figure: Geforce GTX 1080 Undercarriage
What about the future? What is there to come?
High Bandwidth Memory (HBM)

- 3D-stacked DRAM, a.k.a. stack;

Figure: GDDR5 vs HBM (Source: (Stallings, 2015))

- Next generation of graphic cards;

*Logic and Computer Design Fundamentals.*


*Computer Organization and Design: The Hardware/Software Interface.*


*Computer Organization and Architecture.*
Pearson Education.